# On neutrino mass in left-right symmetric theories

Michele Frigerio Service de Physique Théorique - CEA/Saclay

> with Evgeny Kh.Akhmedov, Phys. Rev. Lett. 96 (2006) 061802 JHEP 0701 (2007) 043

SHEP, Southampton, May 4th, 2007





## A master equation





# Outline

- A theoretical perspective on present and future experimental results on the neutrino mass
- From tiny neutrino masses to energy scales beyond the Standard Model: the seesaw mechanism
- A non-minimal well-motivated framework: models with left-right gauge symmetry
- A bottom-up reconstruction of the super-heavy seesaw sector and its implications for
  - \* baryogenesis via leptogenesis
  - \* Grand Unification theories

## Status of oscillations data

### 3 active light neutrinos (no sterile states): a global fit



Mixing angle	Data	$sin^2 \theta_{exp}$ (at 2 $\sigma$ )	$sin^2 \theta_{Tri-Bi-Maximal}$
2-3	Atm - K2K - Minos	0.50(1+0.26/1-0.24)	I/2
1-2	Solar - KamLAND	0.30(1+0.20 1-0.13)	I/3
I-3	Chooz	0.000(+0.025)	0

## Status of oscillations data

### **3 active light neutrinos (no sterile states): a global fit**



σ)	<b>sin<sup>2</sup>θ</b> Tri-Bi-Maximal
	I/2
	I/3
5)	0

### V mass spectrum: open questions

 $\Delta m_{12}^2 \equiv m_2^2 - m_1^2 = 7.9 \cdot 10^{-5} \text{eV}(1 \pm 0.09)$  $\Delta m_{23}^2 \equiv |m_3^2 - m_2^2| = 2.4 \cdot 10^{-3} \text{eV}(1^{+0.21}_{-0.26})$ 

- Future oscillation experiments may measure sign(m<sub>3</sub><sup>2</sup> m<sub>2</sub><sup>2</sup>)
- Absolute mass scale m<sub>i</sub> unknown, but constrained by:
  - tritium  $\beta$  decay:  $m_i < 2.2 \text{ eV}$  [Katrin 3 years:  $m_i < 0.2 \text{ eV}$ ]
  - neutrinoless  $2\beta$  decay:  $m_{ee} < (0.3 \div 1.0) eV$ [Cuoricino & Nemo-3:  $m_{ee} < 0.1 \text{ eV}$ ]
  - cosmological bounds:  $\Sigma_i m_i < (0.4 \div 0.7) \text{ eV}$ [Planck CMB + lensing:  $\sigma(\Sigma_i m_i) \approx 0.05 \text{ eV} \Rightarrow m_i \text{ determined!}$ ]
- If neutrinos are Majorana, two unknown CP violating phases arg(m<sub>1</sub>/m<sub>2</sub>) (enters m<sub>ee</sub>) and arg(m<sub>3</sub>/m<sub>2</sub>) (not accessible)

## Neutrino mass matrix

The most sound theoretical interpretation of all neutrino data: add to the Standard Model a 3x3 Majorana mass term

 $m_{\nu} = U diag(m_1, m_2, m_3) U^{T'}, \quad U = U(\theta_{12}, \theta_{23}, \theta_{13}, \delta)$ 

• Knowns:  $\theta_{12}$ ,  $\theta_{23}$ ,  $m_2^2$  -  $m_1^2$  and  $|m_3^2$  -  $m_2|^2$ ; upper bounds on  $\theta_{13}$  and  $|\mathbf{m}_i|$ .

• Unknowns:  $\theta_{13}$ , sign(m<sub>3</sub><sup>2</sup> - m<sub>2</sub><sup>2</sup>),  $|m_i|$  and three CP phases,  $\delta$ ,  $arg(m_1/m_2)$ ,  $arg(m_3/m_2)$ 

The structure of m<sub>v</sub> provides a crucial clue on the particle theory beyond the Standard Model

Theoretical priorities = fix the largest uncertainties in the structure of  $m_{\nu}$ : (I) mass spectrum (II) Majorana CP phases (III) mixing angles (IV) Dirac CP phase



# What V physics beyond SM?

A non-zero Majorana neutrino mass may be introduced as the effect of the unique dimension 5 effective operator:



### A host of new physics candidates brings a contribution to neutrino mass through this operator: $m_{\nu} =$

## Seesaw mechanisms

**Seesaw** means to interpret the effective operator as the exchange of a certain super-heavy particle



Minkowski, Gell-Mann, Ramond, Slansky, Yanagida, Glashow, Mohapatra, Senjanovic, Magg, Wetterich, Lazarides, Shafi, Schecter, Valle, Foot, Lew, He, Joshi, Ma

> **Seesaw Mechanism** in 3 possible versions: [type I] SM singlet fermions  $N_R$  :  $m_v \sim v^2 / M_R$ [type II] SU(2)<sub>L</sub> triplet scalars  $\Delta$  :  $m_v \sim v^2 / M_\Delta$ [type III] SU(2)<sub>L</sub> triplet fermions  $\Sigma$  :  $m_v \sim v^2 / M_{\Sigma}$



## From a mechanism to a theory

Seesaw explains (i) smallness of v mass (ii) **baryogenesis** via leptogenesis

However the heavy scale and the new particles are ad hoc...

minimal Left-Right gauge symmetry:  $SU(2)_{L} \times SU(2)_{R} \times U(1)_{B-L} \rightarrow SU(2)_{L} \times U(1)_{Y}$ extensions:  $SU_{422}$ , SO(10), ...

(i) **right-handed neutrinos** are incorporated naturally (ii) maximal parity violation can be understood (iii) Grand Unification gives a rationale for the heavy scale (iv) supersymmetry can be easily incorporated & **R-parity** is unbroken [if only (B-L)-even Higgs bosons acquire VEVs]



Pati, Salam, Mohapatra, Senjanovic, Georgi, Fritzsch, Minkowski

# Left-Right symmetric V mass

Fields:	L = (v, e)	$L^{c} = (N^{c}, e^{c})$	$\Phi = (H_u, H_d)$	$\Delta_{L}$	$\Delta_{R}$
SU(2)	2	l	2	3	
SU(2) <sub>R</sub>		2	2		3
U(I) <sub>B-L</sub>	-1		0	2	-2

Lepton Yukawas:  $\mathcal{L}_Y = yLL^c\Phi + \frac{f}{2}(LL\Delta_L + L^cL^c\Delta_R)$ (both y and f are 3x3 symmetric matrices) VEVs:  $-\mathbf{v}_{\mathbf{R}} = \langle \Delta_{\mathbf{R}}^{0} \rangle$  breaks  $SU_{221}$  into  $SU_{21}$ -  $v = \langle \Phi^0 \rangle$  breaks SU<sub>21</sub> into U(1)<sub>em</sub>

 $-v_{\rm L} = \langle \Delta_{\rm L} \rangle \sim v^2 / M_{\Lambda}$  is induced by EW breaking

Mass matrix in (v, N) basis:  $M_{\nu} = \begin{pmatrix} v_L f & vy \\ vy & v_R f \end{pmatrix}$ 



# Left-Right symmetric seesaw

$$M_{\nu} = \begin{pmatrix} v_L f & vy \\ vy & v_R f \end{pmatrix}$$

Integrating out the super-heavy neutrinos N:

$$m_{\nu} = m_{\nu}^{II} + m_{\nu}^{I} = v_L f - v^2 y$$

Type I and II seesaw contributions to light neutrino masses are strictly intertwined

Several Left-Right models which are fully consistent up to GUT scale do not contain other sources of v mass

# Seesaw mechanisms: v << v<sub>R</sub> (Type I) v<sub>L</sub> << v (Type II)

 $(v_R f)$ 

# LR seesaw: the parameter space

$$m_{\nu} = v_L f - v^2 y (v_R f$$

 $v^2 = (174 \text{ GeV})^2$  (EWSB)

- $0 \leq \mathbf{v}_{\mathrm{L}} \leq \mathrm{GeV}$  ( $\Delta \rho \approx -2 \, \mathbf{v}_{\mathrm{L}}^2 / \, \mathbf{v}^2$ )
- TeV  $\leq V_R \leq M_{Pl}$  (no RH weak currents)
- $0 \le (m_v)_{ii} \le eV$  : partially known from oscillations data
  - $0 \le y_{ii} \le 1$ : in general unknown Yukawa couplings, but
    - Minimal SUSY LR:  $y = \tan \beta y_e$
    - Minimal SO(10):  $y = y_u$
    - Seesaw + mSUGRA:  $y_{ij} << I$  to suppress, e.g.,  $\tau \rightarrow \mu \gamma$
- $0 \le f_{ij} \le 1$  : completely unknown Yukawa couplings

**Bottom-up approach: what is the structure of the matrix f?** To what extent we can reconstruct  $M_R = v_R f$ ?

# Seesaw duality

$$m_
u = v_L f$$
 -

Consider a matrix f solution of the seesaw formula for a given set of all other parameters.

Define:  $\hat{f} \equiv \frac{m_{\nu}}{v_{L}} - f$ 

Then:  $m_{\nu} = v_L \hat{f} - v^2 y (v_R \hat{f})^{-1} y$ 

**Duality: f** solution if and only if **f** is

Solutions of the seesaw equation come in pairs:  $f = f_1, \hat{f}_1, f_2, \hat{f}_2, ...$ 





# Multiple solutions

- Seesaw formula **non-linear in f** : for 3 lepton generations, one finds 8 solutions for f (4 dual pairs)
- → The right-handed neutrino mass matrix has 8 possible structures,  $M_R = v_R f$
- $\rightarrow$  For a given y, 8 structures of f induce the same  $m_{y}$
- One may derive a complete analytic resolution of the  $\bullet$ non-linear polynomial system of equations for f<sub>ij</sub>

method 1: Akhmedov & MF method 2: Hosteins, Lavignac & Savoy, NPB 755 (2006) 137



# Full analytic resolution

• Linearize by a rescaling parameter  $\lambda$ :  $f(m_{\alpha\beta}, y_{1,2,3}, v_L, v_R, \lambda)$ 

 $f_{ij} = \frac{\lambda^2 \left[ (\lambda^2 - Y^2)^2 - Y^2 \lambda \det m + Y^4 S \right] m_{ij} + \lambda \left( \lambda^4 - Y^4 \right) A_{ij} - Y^2 \lambda^2 (\lambda^2 + Y^2) S_{ij}}{(\lambda^2 - Y^2)^3 - Y^2 \lambda^2 (\lambda^2 - Y^2) S - 2Y^2 \lambda^3 \det m}$ 

$$Y^2 \equiv rac{(y_1 y_2 y_3)^2}{x^3}\,, \ \ S \equiv \sum_{k,l=1}^3 \left(rac{m_{kl}^2 x}{y_k y_l}
ight)\,, \ \ A_{ij} \equiv rac{y_i y_j M_{ij}}{x}\,, \ \ S_{ij}$$
 $x \equiv v_L v_R/v^2 \quad m \equiv m_
u/v_L \quad M_{ij} \equiv 0$ 

• Non-linearity contained in a 8th order equation for  $\lambda$ 

- $$\begin{split} 0 &= \left[ (\lambda^2 Y^2)^2 Y^2 \lambda^2 S \right]^2 \lambda^2 (\lambda^2 + Y^2)^2 A \\ -Y^2 \lambda^4 (\det m)^2 \lambda \left[ \lambda^6 + Y^2 \lambda^2 (\lambda^2 Y^2) \left( 5 + S \right) Y^6 \right] \det m \end{split}$$
- Seesaw duality  $\Rightarrow$  4th order equation in  $z \equiv \lambda Y^2/\lambda$
- $0 = z^4 \det m \, z^3 (2Y^2S + A)z^2 Y^2(8 + S) \det m \, z + Y^2[Y^2S^2 4A (\det m)^2]$



# A realistic numerical example



 $v_L v_R = v^2$  (natural when scalar potential couplings are of order 1) neglect CKM-like rotations (both charged lepton and neutrino Yukawa couplings diagonal in the same basis)  $y_1 = 10^{-2}$   $y_2 = 10^{-1}$   $y_3 = 1$  (inter-generation hierarchy analog to charged fermions)

 $m_{\nu} = v_L f - v^2 y (v_R f)^{-1} y$  the 4 dual pairs of f

- **Tribimaximal** mixing:
- $\tan^2 \theta_{23} = 1$
- $\tan^2 \theta_{12} = 0.5$
- $\tan^2 \theta_{13} = 0$
- **No CP violation**

ΕX

## Given all these inputs, structures are determined

## The 8 reconstructed solutions



## Features of the solutions

### Consider a given pair of dual solutions:

 $f_4 \approx \begin{pmatrix} -0.001 & 0.105 & -0.14 \\ \dots & 0.56 & 0.49 \\ \dots & \dots & 0.88 \end{pmatrix} \qquad \hat{f}_4 \approx \begin{pmatrix} 0.001 & -0.005 & 0.04 \\ \dots & -0.01 & -0.04 \\ \dots & \dots & -0.33 \end{pmatrix}$ Seesaw Duality:  $f_4 + \hat{f}_4 = m = \begin{pmatrix} 0 & 0.1 & -0.1 \\ \dots & 0.55 & 0.45 \\ \dots & \dots & 0.55 \end{pmatrix}$ **f**<sub>4</sub> **structure** has dominant 23-block; large (but non-maximal) 2-3 mixing

**One seesaw type dominance** in  $m_{12}$ ,  $m_{22}$ ,  $m_{23}$ : type II in the case of  $f_4$ , type I in the dual case. Mixed seesaw in  $m_{11}$ ,  $m_{13}$ ,  $m_{33}$ .

### **Dual structure** is hierarchical, with dominant 33-entry; small 2-3 mixing

## Right-handed neutrino masses

### as a function of the absolute scale of light neutrino masses



Normal hierarchy

Solution f<sub>4</sub>: solid lines Solution dual to f<sub>4</sub>: dashed lines

 $m_1 (eV)$ 0.2

Quasi-degeneracy

# Right-handed neutrino masses

### as a function of the Left-Right symmetry breaking scale v<sub>R</sub>



# Recipes for light RH neutrinos

Interesting for (i) active-sterile oscillations (ii) warm dark matter [Shaposhnikov, ...] (iii) low scale leptogenesis (iv) direct detection at LHC [Del Aguila, ...]

- Assume tiny first generation Yukawa coupling:  $M_1 \sim y_1^2$
- Lower left-right symmetry breaking scale  $v_R$  at few TeVs with  $v_L v_R << v^2$ ; it follows  $y_i < 10^{-5}$  and  $M_i \sim v_R$
- Lower  $v_R$  keeping  $v_L v_R \approx v^2$ ; both y and f couplings need to be very small:  $M_i \ll v_R$
- Take  $v_R$  at few TeVs with couplings y of order one arranged in such a way to cancel in type I seesaw



# Baryogenesis via Leptogenesis



- Majorana mass term  $M_R N N$  for super-heavy neutrinos  $N_i$ violates Lepton Number
- $N_{I}$  decays at T  $\approx M_{I}$  out-of-equilibrium generating a lepton asymmetry by the interference between decay amplitudes at tree level and I-loop:  $\epsilon_L \sim [\Gamma(N_1 \rightarrow LH) - \Gamma(N_1 \rightarrow L^*H^*)]$
- Standard Model B+L violating effects at T > v convert lepton into baryon asymmetry. Since  $[n_B/s]_{exp} \approx 10^{-10} \leq 10^{-3} \in L$ , one needs  $\epsilon_{L} \geq 10^{-7} \div 10^{-6}$



# Leptogenesis in Left-Right models

- The needed lepton asymmetry may be produced either by the type I seesaw sector ( $N_i$  decays), by the type II seesaw sector ( $\Delta_L$  decays), or by their interplay.
- LR symmetry implies that the same matrix f determines both N<sub>i</sub> masses and  $\Delta_L$  coupling to leptons: more predictivity
- The 8 possible structures of f can be discriminated by their ability to achieve Baryogenesis via Leptogenesis
- Seesaw duality provides new options to enhance the asymmetry: (i) solutions where  $M_R$  is not hierarchical, (ii) solutions with quasi-degenerate masses, (iii) extra sources of asymmetry in the LR breaking sector, ...

Detailed studies by: Hosteins, Lavignac & Savoy, NPB 755 (2006) 137; Akhmedov, Blennow, Hallgren, Konstandin, Ohlsson, hep-ph/0612194.

# Multiple options for leptogenesis

### Hosteins, Lavignac & Savoy, NPB 755 (2006) 137





# Grand Unification à la SO(10)

 $SU(3)_c \times [SU(2)_L \times SU(2)_R \times U(1)_{B-L}] \subset SO(10)$ 

All SM fermions + N's sit in the same multiplet  $16_F$ 

Neutrino Majorana masses from a unique coupling:

 $f \mathbf{16}_F \mathbf{16}_F \mathbf{16}_F \mathbf{176}_H \ni f(LL\Delta_L + L^c L^c \Delta_R)$ 

Neutrino Dirac masses can receive several contributions:

 $vy = \langle \mathbf{10}_H \rangle y_{10} + \langle \mathbf{120}_H \rangle y_{120} + \langle \mathbf{126}_H \rangle f$ 

Even if f contributes to y the seesaw can be written as:

$$m'_{\nu} = v_L f - v^2 y' (v_R f)^{-1}$$

Therefore there are always multiple solutions for f. Duality holds if only 10s and 126s (only 120s) contribute to y.

# Minimal Supersymmetric SO(10)

### **Renormalizable Yukawas from one 10<sub>H</sub> and one 126<sub>H</sub> only**

Babu, Mohapatra, Clark, Kuo, Nakagawa, Bajc, Senjanovic, Vissani, Melfo, Aulakh, Girdhar, Macesanu, Goh, Ng, Dutta, Mimura, Bertolini, Frigerio, Malinsky, ...

$$\mathcal{L}_Y = \mathbf{16}_F \left( y \, \mathbf{10}_H + f \, \overline{\mathbf{126}}_H \right) \mathbf{16}_F$$

However, y and f strongly constrained by charged fermion masses and CKM mixing angles

The global fit of fermion masses and mixing (including neutrinos) is intricate and very constrained.

Most recent analysis: a perfect fit is possible, but the required heavy mass spectrum is incompatible with gauge coupling unification.

> Bertolini, Malinsky & Schwetz, PRD 73 (2006) 115012 (see also Aulakh & Garg, NPB 757 (2006) 47)

Neutrino sector:  $y = y_u$   $\Rightarrow$  8 solutions for f



# Non-minimal SUSY SO(10)

### **126<sub>H</sub> plus two 10<sub>H</sub> multiplets**

Hosteins, Lavignac & Savoy, hep-ph/0606078

1) Up versus down: two  $10_H$  distinguish vy = M<sub>u</sub> from  $M_d = M_e$ 2) The 8 dual solutions for f may be derived from neutrino sector 3) For each viable f, one may compute (i) lepton asymmetry (ii) lepton flavor violation bounds (iii) correction to  $M_d \neq M_e$ , which remains difficult

**126**<sub>H</sub> plus one  $10_H$  and one  $120_H$ 

Aulakh, hep-ph/0602132, 0607252 Grimus, Kuhbock, Lavoura, hep-ph/0603259, 0607197

1) Fit with  $10_{\rm H}$  and  $120_{\rm H}$  alone  $M_{\rm H}$ ,  $M_{\rm d}$  and  $M_{\rm e}$ (there is some small tension for first generation masses). 2) Derive the 8 dual solutions for f from neutrino sector 3) Select the (possibly) unique structure for f which achieves a good fit of m<sub>e</sub>, m<sub>u</sub>, m<sub>d</sub>.



• The understanding of neutrino mass relies on the identification of its dominant source.

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- If the new physics if Left-Right symmetric, type [+]] seesaw stands up firmly as the unique candidate.
- Bottom-up reconstruction of the superheavy seesaw sector: duality among 8 different structures.
- Numerical & analytic reconstruction of the 8 structures allows to investigate different options for:
- Baryogenesis via Leptogenesis
- Grand Unified Theories
- flavor symmetries, lepton flavor violation, etc...